

6. Express (i) 2^{x+2} and (ii) $2^x + 2^x$ in the form $k2^x$, where $k \in \mathbb{N}$.
 (iii) Hence solve for c in the equation $2^x + 2^x = 2^{x+2}(c - 2)$.

(i)	$2^{x+2} = 2^x \cdot 2^2 = 4(2^x)$
$a^{n+m} = a^n \cdot a^m$	
(ii)	$2^x + 2^x = 2(2^x)$
$a+a = 2a$	
(iii)	$2^x + 2^x = 2^{x+2}(c-2)$
$\div 4(2^x)$	$2(2^x) = 4(2^x)(c-2)$
$+2$	$\frac{1}{2} = c-2$
	$c = \frac{1}{2} + 2 = \frac{5}{2}$
	$c = \frac{5}{2}$

10. If $y = 2^x$, write (i) 2^{2x} (ii) 2^{2x+1} and (iii) 2^{x+3} in terms of y .
 (iv) Hence solve the equation $2^{2x+1} - 2^{x+3} - 2^x + 4 = 0$.

$y = 2^x$	(i)	$2^{2x} = (2^x)^2 = y^2$
$a^{n+m} = a^n \cdot a^m$	(ii)	$2^{2x+1} = (2^{2x})(2) = 2y^2$
	(iii)	$2^{x+3} = (2^x)(2^3) = 8y$
	(iv)	$2^{2x+1} - 2^{x+3} - 2^x + 4 = 0$
Sub in y		$2y^2 - 8y - y + 4 = 0$
Simplify		$2y^2 - 9y + 4 = 0$
		$(2y-1)(y-4) = 0$
		$2y-1=0 \quad \quad y=4$
		$y = \frac{1}{2}$
$x=?$		$\frac{1}{2} = 2^x \Rightarrow x = -1$
$y = 2^x$		$4 = 2^x \Rightarrow x = 2$

11. By using the substitution $y = 3^x$, find the two values of x such that $3 \cdot 3^x + 3^{-x} = 4$ and verify each solution by substitution into the original exponential equation.

$\text{let } y = 3^x$	$3(3^x) + 3^{-x} = 4$
	$3y + \frac{1}{y} = 4$
$\times y$	$3y^2 + 1 = 4y$
	$3y^2 - 4y + 1 = 0$
	$(3y - 1)(y - 1) = 0$
	$3y - 1 = 0 \quad \quad y = 1$
	$y = \frac{1}{3}$
$y = 3^x, \quad x = ?$	$\frac{1}{3} = 3^x \quad \Rightarrow \quad x = -1$
	$1 = 3^x \quad \Rightarrow \quad x = 0$