

7. A farmer buys a tractor for €180 000.  
He assumes that the tractor will have a trade-in value of €80 000 in 10 years time.
- Calculate the rate of depreciation per annum, correct to one place of decimals, based on these figures.
  - At this rate, when will the value of the tractor fall below €60 000?

$$F = P(1-i)^t \quad (i)$$

$$\frac{F}{P} = (1-i)^t$$

$$\sqrt[t]{\frac{F}{P}} = 1-i$$

$$t = \log_{(1-i)} \frac{F}{P}$$
  

$$P = 180\,000$$

$$F = 80\,000$$

$$t = 10$$

$$i = ?$$
  

$$1-i = \sqrt[10]{\frac{80\,000}{180\,000}} = 0.9221$$

$$\Rightarrow 1-0.9221 = i = 0.0778$$

$$i = 7.78\% \approx 7.8\%$$
  

$$P = 180\,000$$

$$F = 60\,000$$

$$t = ?$$

$$i = 7.8\%$$
  

$$t = \log_{0.9221} \left( \frac{60\,000}{180\,000} \right)$$

$$\approx 13.546 \text{ years}$$

$$t \approx 13 \text{ years}$$