

In a complex equation:
 $Re = Re$ and $Im = Im$

If $a + bi = x + yi$,
 then $a = x$ and $b = y$

Example 2

Find x and y if $\underbrace{x + 2i}_{LHS} + 2(3 - 5yi) = \underbrace{8 - 13i}_{RHS}$.

Tidy LHS	$x + 2i + 2(3 - 5yi) = 8 - 13i$ $x + 2i + 6 - 10yi = 8 - 13i$
$Re = Re$	$x + 6 = 8 \quad \Rightarrow \quad \boxed{x = 2}$
$Im = Im$	$2i - 10yi = -13i$ $+10y = +15$ $y = 15/10 \quad \boxed{y = 3/2}$

7. Find the values of a and b in each of the following:

(i) $a + bi + 3 - 2i = 4(-2 + 5i)$

Expand RHS	$a + bi + 3 - 2i = 4(-2 + 5i)$ $a + bi + 3 - 2i = -8 + 20i$
$Re = Re$	$a + 3 = -8 \quad \Rightarrow \quad \boxed{a = -11}$
$Im = Im$	$b - 2 = 20 \quad \Rightarrow \quad \boxed{b = 22}$

11. If $(x + iy)^2 = 8 - 6i$, find the values of x and y , $x, y \in \mathbb{R}$.

expand RHS

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$\operatorname{Re} = \operatorname{Re}$$

$$\operatorname{Im} = \operatorname{Im}$$

$$(x + iy)^2 = 8 - 6i$$

$$x^2 + 2xyi + y^2i^2 = 8 - 6i$$

$$x^2 - y^2 = 8$$

$$2xy = -6$$