



Section 2.8 Algebraic surd equations

PROJECT MATHS
Text & Tests 6

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4. Show that $\frac{-1 + \sqrt{3}}{1 + \sqrt{3}} = 2 - \sqrt{3}$.

multiply
above and
below by
conjugate of
denominator

$$\begin{aligned}
 & \frac{(-1 + \sqrt{3})(1 - \sqrt{3})}{(1 + \sqrt{3})(1 - \sqrt{3})} \\
 & \quad \text{Dots} \\
 & \frac{-1 + \sqrt{3} + \sqrt{3} - 3}{1 - 3} \\
 & = \frac{-4 + 2\sqrt{3}}{-2} = \frac{-4}{-2} + \frac{2\sqrt{3}}{-2} \\
 & = 2 - \sqrt{3}
 \end{aligned}$$

5. Express $\frac{\sqrt{3}}{1-\sqrt{3}} - \frac{1}{\sqrt{3}}$ as a single fraction and simplify by rationalising the denominator.

Bow Tie

RATIONALISE

FOIL

$$\begin{aligned}
 & \frac{\sqrt{3}(\sqrt{3}) - 1(1-\sqrt{3})}{(1-\sqrt{3})(\sqrt{3})} \\
 & \frac{3 - 1 + \sqrt{3}}{\sqrt{3} - 3} \\
 & = \frac{(2 + \sqrt{3})(-3 - \sqrt{3})}{(-3 + \sqrt{3})(-3 - \sqrt{3})} \quad \text{dots} \\
 & = \frac{-6 - 2\sqrt{3} - 3\sqrt{3} - 3}{9 - 3} \\
 & = \frac{-9 - 5\sqrt{3}}{6}
 \end{aligned}$$

7. Solve the following equations and check your solutions in each case:

(i) $\sqrt{2x+1} = 3$

(ii) $\sqrt{3x+10} = x$

(iii) $\sqrt{2x-1} = \sqrt{x+8}$

Square

(i)

$$\begin{aligned}
 \sqrt{2x+1} &= 3 \\
 2x+1 &= 9 \\
 2x &= 8 \\
 x &= 4
 \end{aligned}$$

$$\begin{aligned}
 \text{check } \sqrt{2(4)+1} &= \sqrt{9} \\
 &= 3 \quad \checkmark
 \end{aligned}$$

Square

(ii)

check : $x = -2$

$$\begin{aligned}
 \sqrt{3x+10} &= x \\
 3x+10 &= x^2 \\
 x^2 - 3x - 10 &= 0 \\
 (x+2)(x-5) &= 0 \\
 x = -2 \text{ or } x &= 5
 \end{aligned}$$

$$\begin{aligned}
 \sqrt{3(-2)+10} &\stackrel{?}{=} -2 \\
 \sqrt{-6+10} &\stackrel{?}{=} -2 \\
 \sqrt{4} &\stackrel{?}{=} -2 \\
 2 &\stackrel{?}{=} -2 \quad \text{not true} \Rightarrow \text{reject.}
 \end{aligned}$$

 $x = 5$

$$\begin{aligned}
 \sqrt{3(5)+10} &\stackrel{?}{=} 5 \\
 \sqrt{25} &= 5 \quad \checkmark \text{ true}
 \end{aligned}$$