



Section 1.5 Algebraic identities

(IDEA) if $2x^3 + 3x^2 - 4 = ax^3 + bx^2 + cx + d$

then $a = 2$
 $b = 3$
 $c = 0$
 $d = -4$

19

PROJECT MATHS
Text & Tests 6

Example 1

Find the values of a and b given that $(2x + a)^2 = 4x^2 + 12x + b$, for all values of x .

$$(a+b)^2 = a^2 + 2ab + b^2$$

expand LHS

$$\begin{array}{lcl} (2x+a)^2 & = & 4x^2 + 12x + b \\ 4x^2 + 4xa + a^2 & = & 4x^2 + 12x + b \end{array}$$

IDENTITIES \Rightarrow

$$4a = 12 \quad | \quad a^2 = b \quad (2)$$

$$a = 3 \quad (1)$$

Sub (1) into (2)

$$(3)^2 = b$$

$$b = 9$$

Example 2

If $3t^2x - 3px + c - 2t^3 = 0$ for all values of x , find c in terms of p .

LINEAR EXPRESSION

IDENTITY

$$3t^2x - 3px + c - 2t^3 = 0$$

$$(3t^2 - 3p)x + (c - 2t^3) = 0x + 0$$

X coefficients \Rightarrow

$$3t^2 - 3p = 0$$

$$3t^2 = 3p$$

$$t^2 = p \quad \textcircled{1} \quad \Rightarrow \quad t = \sqrt{p}$$

Constant terms \Rightarrow

$$c - 2t^3 = 0$$

$$c = 2t^3 \quad \textcircled{2}$$

$$c = ?$$

Sub $\textcircled{1}$ into $\textcircled{2}$

$$c = 2(\sqrt{p})^3$$

$$\text{or } c = 2p^{3/2}$$

Example 3

Given $\frac{1}{(x+1)(x-2)} = \frac{A}{(x+1)} + \frac{B}{(x-2)}$ for all values of x , find the values of A and B .

LCD = $(x+1)(x-2)$
MULTIPLY BY LCD

$$\frac{1}{(x+1)(x-2)} = \frac{A(x+1)(x-2)}{(x+1)} + \frac{B(x+1)(x-2)}{(x-2)}$$

$$1 = A(x-2) + B(x+1)$$

$$1 = Ax - 2A + Bx + B$$

LINEAR

$$1 = (A+B)x + (B-2A)$$

$$0x + 1 = (A+B)x + (B-2A)$$

\Rightarrow

$$\begin{aligned} 0 &= A+B \\ A &= -B \end{aligned} \quad \textcircled{1}$$

$$1 = B - 2(-B) \quad \textcircled{2}$$

Sub $\textcircled{1}$ into $\textcircled{2}$

$$1 = B - 2(-B)$$

$$1 = B + 2B$$

$$1 = 3B$$

$$B = 1/3 \quad \Rightarrow \quad A = -1/3$$