

Algebra 1

chapter

1

Section 1.3 Factorising algebraic expressions

PROJECT MATHS
Text & Tests 6

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Factorising

$$a^2 - b^2 = (a - b)(a + b)$$

*learn

① HCF

② Grouping

③ Quadratic

④ D.O.T.S.

⑤ Difference of 2 cubes (D.O.T.C.)

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

⑥ Sum of 2 cubes (S.O.T.C.)

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

Example 4

Factorise (i) $a^3 + 8b^3$ (ii) $64c^3 - 125d^3$

(i) *Sum of 2 cubes*

$$x^3 + y^3 = (x+y)(x^2 - xy + y^2)$$

$$x^3 = a^3$$

$$x = a$$

$$y^3 = 8b^3$$

$$y = 2b$$

$$\begin{aligned} a^3 + 8b^3 &= (a + 2b)(a^2 - (a)(2b) + (2b)^2) \\ &= (a + 2b)(a^2 - 2ab + 4b^2) \end{aligned}$$

(ii) *Difference 2 cubes*

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$a^3 = 64c^3$$

$$a = 4c$$

$$b^3 = 125d^3$$

$$b = 5d$$

$$\begin{aligned} 64c^3 - 125d^3 &= (4c - 5d)((4c)^2 + (4c)(5d) + (5d)^2) \\ &= (4c - 5d)(16c^2 + 20cd + 25d^2) \end{aligned}$$