

Probability distributions

Binomial distribution:

$$P(r) = \binom{n}{r} p^r q^{n-r}$$

$$\mu = np$$

$$\sigma = \sqrt{npq}$$

Poisson distribution:

$$P(r) = e^{-\lambda} \frac{\lambda^r}{r!}, \quad \lambda = np$$

$$\mu = \lambda$$

$$\sigma = \sqrt{\lambda}$$

Normal (Gaussian) distribution:

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

Standard normal distribution:

$$f(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}$$

Standardising formula: $z = \frac{x - \mu}{\sigma}$

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Binomial coefficients

$$\binom{n}{r} = {}^n C_r = C(n, r) = \frac{n!}{r!(n-r)!}$$

Some values of ${}^n C_r$:

$n \setminus r$	0	1	2	3	4	5	6	7	8
0	1								
1	1	1							
2	1	2	1						
3	1	3	3	1					
4	1	4	6	4	1				
5	1	5	10	10	5	1			
6	1	6	15	20	15	6	1		
7	1	7	21	35	35	21	7	1	
8	1	8	28	56	70	56	28	8	1
9	1	9	36	84	126	126	84	36	9
10	1	10	45	120	210	252	210	120	45
11	1	11	55	165	330	462	462	330	165
12	1	12	66	220	495	792	924	792	495
13	1	13	78	286	715	1287	1716	1716	1287
14	1	14	91	364	1001	2002	3003	3432	3003
15	1	15	105	455	1365	3003	5005	6435	6435

28. The chest measurements of teenage male customers for T-shirts may be modelled by a normal distribution with mean 101 cm and standard deviation 5 cm. Find the probability that a randomly-selected customer will have a chest measurement which is
- (i) less than 103 cm
 - (ii) 98 cm or more
 - (iii) between 95 and 100 cm.

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$$z = \frac{x - \mu}{\sigma}$$

$\mu = 101 \text{ cm}$
 $\sigma = 5 \text{ cm}$

(i) $P(X < 103 \text{ cm}) = ?$
 $z = \frac{103 - 101}{5} = \frac{2}{5} = 0.4$
 $P(z < 0.4) = 65.54\%$

(ii) $P(X > 98 \text{ cm}) = ?$
 $z = \frac{98 - 101}{5} = \frac{-3}{5} = -0.6$
 $P(z > -0.6) = P(z < 0.6) = 72.57\%$

(iii) $X = 95 \Rightarrow z = \frac{95 - 101}{5} = \frac{-6}{5} = -1.2$
 $X = 100 \Rightarrow z = \frac{100 - 101}{5} = \frac{-1}{5} = -0.2$
 $P(-1.2 < z < -0.2) = P(0.2 < z < 1.2) = P(z < 1.2) - P(z < 0.2)$
By symmetry
 $= 88.49\% - 57.93\% = 30.56\%$