

Probability 1

chapter 1

Section 1.6 The multiplication law for independent events

- If A is independent of B the probability of one doesn't depend on the other.
- If A is not independent of B its probability is 'CONDITIONAL'



Paul spins a coin  and rolls a dice. 

His results are shown on the right.

The coin and the dice do not affect each other, so their outcomes are **independent**.

There are 12 equally likely outcomes of the coin and dice, as shown in the diagram on the right.

From the sample space, we can see that the probability of a head and a 5 is $\frac{1}{12}$.

The probability of each outcome can also be found by multiplying the separate probabilities, as shown above.

6	H, 6	T, 6
5	H, 5	T, 5
4	H, 4	T, 4
3	H, 3	T, 3
2	H, 2	T, 2
1	H, 1	T, 1
	H(ead)	T(ail)
	Coin	

This illustrates the **multiplication law** of probability which states that for independent events A and B,

$$P(A \text{ and } B) = P(A) \times P(B)$$

This law is sometimes called the AND Rule.

The multiplication law applies to any number of independent events.

Example 1

When two dice are thrown, what is the probability of getting

- (i) two sixes (ii) 4 or more on each die?

Multiply

$$P(4 \text{ or more}) = 3/6 = 1/2$$

SAMPLE SPACE

	1	2	3	4	5	6
1
2
3
4
5
6

$$P(6,6) = P(6) \times P(6) \\ = \frac{1}{6} \times \frac{1}{6} = \frac{1}{36}$$

$$P(4 \text{ or more}, 4 \text{ or more}) \\ = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$