



$$\sum_{r=0}^5 2^r \quad ?$$

term rule

$$\sum_{r=0}^5 2^r = 2(0) + 2(1) + 2(2) + 2(3) + 2(4) + 2(5) = 30$$

$$\begin{aligned} \sum_{r=0}^{20} 2^r &= 2(0) + 2(1) + 2(2) + \dots + 2(20) \\ &= 0 + 2 + 4 + \dots + 40 \end{aligned}$$

$T_1 = a$
 $d = +2$

Arithmetic
Sum

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\begin{aligned} S_{21} &= \frac{21}{2} [2(0) + (20)2] \\ &= 420 \end{aligned}$$

Arithmetic Sequence "d"

$$T_5 = -18, T_{10} = 12$$

$$a = ?$$

$$d = ?$$

$$S_{15} = ?$$

$$T_5 = -18$$

$$T_{10} = 12$$

$$T_n = a + (n-1)d$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$a + 4d = -18 \quad ①$$

$$+ a + 9d = +12 \quad ②$$

$$- 5d = -30$$

$$d = 6$$

→ ①

$$a + 4(6) = -18$$

$$a = -42$$

$$S_{15} = \frac{15}{2} [2(-42) + (15-1)6]$$

$$S_{15} = 0$$

Find Three no.s in an arithmetic sequence:

$$\text{Sum} = 27, \text{ Product} = 704. ?$$

$$T_n = a + (n-1)d$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

let nos be $a, a+d, a+2d$

$$\text{Sum} = 27$$

$$a + a+d + a+2d = 27$$

$$3a + 3d = 27$$

$$a+d = 9 \Rightarrow a = 9-d$$

$$\text{Product} = 704$$

$$(a)(a+d)(a+2d) = 704$$

$$\Rightarrow (9-d)(9-d+d)(9-d+2d) = 704$$

$$(9-d)(9+d) = 704$$

$$9(81-d^2) = 704$$

$$81-d^2 = \frac{704}{9}$$

$$81-\frac{704}{9} = d^2 \quad \text{2 options}$$

$$d = \sqrt{81-\frac{704}{9}} = \pm \frac{5}{3}$$

$$\text{if } d = \frac{5}{3} \Rightarrow a = 9 - \frac{5}{3} = \frac{22}{3}$$

$$\text{Sequence: } \frac{22}{3}, 9, \frac{32}{3}$$

$$\text{or if } d = -\frac{5}{3}$$

$$\text{Sequence: } \frac{32}{3}, 9, \frac{22}{3}$$